

pgcd (subres) [XGCD]

$$u \cdot v = (t, v) \rightarrow \text{pgcd}(u, v)$$

$$\deg(u) \geq \deg(v)$$

$x =$  1<sup>er</sup> var de  $u$  et  $v$

$$u = a_m x^m + \dots + a_0$$

$$v = b_n x^n + \dots + b_0$$

$$\alpha = \text{cont}(u) = \text{pgcd}(a_m, \text{pgcd}(a_{m-1}, \dots, a_0))$$

$$\beta = \text{cont}(v) = \text{pgcd}(b_n, \dots, b_0)$$

$$d = \text{pgcd}(\alpha, \beta)$$

$$\text{si } \deg(u) = 0 \rightarrow d$$

$$u = u/\alpha$$

$$v = v/\beta$$

$$g = 1$$

$$h = 1$$

$$B \cdot u = qv + r \quad \} \rightarrow S, B = l(x), q, r$$

$$r = 0$$

$$\deg(r) = 0$$

$$d = \text{cont}(v)$$

$$\text{pgcd} = \frac{r}{\alpha} \cdot d$$

$$u = v$$

$$v = r/g \cdot h^s$$

$$g = B$$

$$s = 0$$

$$s = 1$$

$$m$$

$$a = g^s$$

$$b = h^{s-1}$$

$$h = a/b$$

